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Paper Id: 199243

	Su	ıb C	`od€	e: K	AS	203		
Roll No.								

B. TECH. (SEM II) THEORY EXAMINATION 2018-19 MATHEMATICS-II

Time: 3 Hours Total Marks: 100

Note: Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

1. Attempt all questions in brief.

 $2 \times 10 = 20$

QNo.	Question	Marks	CO
a.	Find the P.I of $\frac{d^2y}{dx^2} + 4y = \sin 2x$	2	1
b.	Solve simultaneous equations $\frac{dx}{dt} = 3y$, $\frac{dy}{dt} = 3x$	2	1
c.	Find the volume of solid generated by revolving the circle $x^2 + y^2 = 25$	2	2
	about <i>y</i> -axis.		
d.	Evaluate $\Gamma\left(-\frac{5}{2}\right)$. where Γ is gamma function	2	2
e.	Find the Fourier constant a_1 of $f(x) = x^2$, $-\pi \le x \le \pi$	2	3
f.	Discuss the convergence of sequence $a_n = \frac{2n}{n^2+1}$.	2	3
g.	Show that complex function $f(z) = z^3$ is analytic.	2	4
h.	Define Conformal mapping.	2	4
i.	Evaluate $\int_0^{1+i} (x^2 - iy) dz$ along the path $y = x$.	2	5
j.	Find residue of $f(z) = \frac{\cos z}{z(z+5)}$ at $z=0$	2	5

SECTION B

2. Attempt any *three* of the following:

QNo.	Question	Marks	CO
a.	Use Frobenius method to solve $9x(1-x)\frac{d^2y}{dx^2} - 12\frac{dy}{dx} + 4y = 0$	10	1
b.	Apply Dirichlet integral to find the volume of an octant of the sphere $x^2 + y^2 + z^2 = 25$.	10	2
c.	Find half range sine series of $f(x) = \begin{cases} x & 0 < x < 2 \\ 4 - x & 2 < x < 4 \end{cases}$	10	3
d.	Show that $u = x^4 - 6x^2y^2 + y^4$ is harmonic function. Find complex function $f(z)$ whose u is a real part.	10	4
e.	Expand $f(z) = \frac{1}{(z-1)(z-2)}$ in regions	10	5
	(i) 1 < z < 2 $(ii) 2 < z $		

SECTION C

3. Attempt any *one* part of the following:

QNo.	Question	Marks	CO
a.	Solve $\frac{d^2y}{dx^2} + y = tanx$ by method of variation of parameter.	10	1

b.	Solve $x^2 \frac{d^2y}{dx^2} - 2(x^2 + x) \frac{dy}{dx} + (x^2 + 2x + 2)y = 0$ by Normal Form.	10	1	
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4. Attempt any *one* part of the following:

QNo.	Question	Marks	CO
a.	Prove that $\beta(m,n) = \frac{\Gamma m \Gamma n}{\Gamma(m+n)}$ where Γ is gamma function	10	2
b.	Use Beta and Gamma function to solve $\int_0^\infty \frac{1}{1+x^4} dx \int_0^{\frac{\pi}{2}} \sqrt{\cot \theta} d\theta$	10	2

5. Attempt any *one* part of the following:

QNo.	Question	Marks	CO
a.	Find the Fourier series of $f(x) = x \sin x$, $-\pi \le x \le \pi$	10	3
b.	State D' Alembert's test. Test the series $1 + \frac{x}{2} + \frac{x^2}{5} + \frac{x^3}{10} \dots \dots + \frac{x^n}{n^2+1} + \dots$	10	3

6. Attempt any *one* part of the following:

QNo.	Question	Marks	CO
a.	Let $f(z) = \frac{x^2y^5(x+iy)}{x^4+y^{10}}$ when $z \neq 0$, $f(z) = 0$ when $z = 0$. Prove	10	4
	that Cauchy Riemann satisfies at $z = 0$ but function is not differentiable at $z = 0$.	6	6
b.	Find Mobius transformation that maps points $z = 0, -i, 2i$ into the points $w = 5i, \infty, -\frac{i}{3}$ respectively.	10	4

7. Attempt any *one* part of the following:

QNo.	Question	Marks	CO
a.	Using Cauchy Integral formula evaluate $\int_{c} \frac{\sin z}{(z^2 + 25)^2} dz$ where c is	10	5
h	circle $ z = 8$	10	5
b.	Apply residue theorem to evaluate $\int_{-\infty}^{\infty} \frac{x dx}{(x^2+1)(x^2+4)}$	10	3