



MTECH

(SEM II) THEORY EXAMINATION 2023-24

DETECTION AND ESTIMATIONTHEORY

TIME: 3 HRS

M.MARKS: 70

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

1. Attempt all questions in brief.

 $2 \ge 7 = 14$

 $7 \ge 3 = 21$

 $7 \times 1 = 7$

 $7 \ge 1 = 7$

- What is binary hypothesis testing? a. What is the minimax criterion? b.
- What is signal detection in discrete time? c.
- What is the probability of detection? d.

Define the MMSE estimate. e.

f. Define linear estimation.

Define Gaussian noise. g.

SECTION B

2. Attempt any *three* of the following:

- Explain the differences between Type I and Type II errors, and their a. significance in hypothesis testing
- Explain the methods used for the detection of stochastic signals. b.
- Discuss the fundamental principles of Bayesian parameter estimation and its c.
- advantages over classical methods.
- d. What is the discrete-time Kalman-Bucy filter?

Explain the derivation and application of the matched filter in signal detection e.

SECTION C

Attempt any *one* part of the following: 3.

- Explain how the power of a test is calculated and its importance in hypothesis a. testing.
 - b. Discuss the importance of selecting appropriate priors in Bayesian hypothesis testing. 7 x 1 = 7

4. Attempt any one part of the following:

- Describe the likelihood ratio test and its application in signal detection. a. Explain the concept of signal-to-noise ratio (SNR) and its importance in signal b.
- detection.

Attempt any one part of the following: 5.

- Discuss the principles and steps involved in Maximum Likelihood (ML) a. estimation. You observe a sample x = [1,2,3,4,5], from a normal distribution N (μ, σ^2) , with $\sigma^2=1$. Calculate the MLE for μ .
- Explain the concept of consistency for MLEs and how it is demonstrated in b. large samples. $7 \ge 1 = 7$

Attempt any one part of the following: 6.

Describe the linear estimation process and its applications in signal processing. a. Describe the process of designing a Wiener filter for a given signal estimation b. problem. 7 x 1 = 7

7. Attempt any one part of the following:

Discuss the importance of SNR in evaluating the performance of detection a. systems. Explain the Neyman-Pearson criterion and its application in hypothesis testing. b.